Two-Dimensional Ferroelectric Topological Insulators in Functionalized Atomically Thin Bismuth Layers

Liangzhi Kou  
Queensland University of Technology

Huixia Fu  
Weizmann Institute of Science

Yandong Ma  
Shandong University

Binghai Yan  
Weizmann Institute of Science

Ting Liao  
Queensland University of Technology

Follow this and additional works at: https://digitalscholarship.unlv.edu/physastr_fac_articles

Citation Information  
Two-dimensional ferroelectric topological insulators in functionalized atomically thin bismuth layers

Liangzhi Kou,1,* Huixia Fu,2 Yandong Ma,3 Binghai Yan,2 Ting Liao,1 Aijun Du,1 and Changfeng Chen4

1School of Chemistry, Physics and Mechanical Engineering Faculty, Queensland University of Technology, Garden Point Campus, Brisbane, Queensland 4001, Australia
2Department of Condensed Matter Physics, Weizmann Institute of Science, Rehovot 7610001, Israel
3School of Physics, State Key Laboratory of Crystal Materials, Shandong University, Shandanan Street 27, 250100 Jinan, People’s Republic of China
4Department of Physics and Astronomy and High Pressure Science and Engineering Center, University of Nevada, Las Vegas, Nevada 89154, United States

(Received 6 November 2017; published 20 February 2018)

We introduce a class of two-dimensional (2D) materials that possess coexisting ferroelectric and topologically insulating orders. Such ferroelectric topological insulators (FETIs) occur in noncentrosymmetric atomic layer structures with strong spin-orbit coupling (SOC). We showcase a prototype 2D FETI in an atomically thin bismuth layer functionalized by CH2OH, which exhibits a large ferroelectric polarization that is switchable by a ligand molecule rotation mechanism and a strong SOC that drives a band inversion leading to the topologically insulating state. An external electric field that switches the ferroelectric polarization also tunes the spin texture in the underlying atomic lattice. Moreover, the functionalized bismuth layer exhibits an additional quantum order driven by the valley splitting at the K and K’ points in the Brillouin zone stemming from the symmetry breaking and strong SOC in the system, resulting in a remarkable state of matter with the simultaneous presence of the quantum spin Hall and quantum valley Hall effect. These phenomena are predicted to exist in other similarly constructed 2D FETIs, thereby offering a unique quantum material platform for discovering novel physics and exploring innovative applications.

DOI: 10.1103/PhysRevB.97.075429

I. INTRODUCTION

Recent years have seen the rise of a distinct class of materials that exhibit topologically protected helical metallic edge states while maintaining an insulating bulk, leading to the so-called quantum spin Hall effect (QSHE) [1, 2]. The remarkable properties of these topological insulators (TIs) provide a platform to elucidate fundamental physics principles underlying the new phenomena and explore innovative applications [3, 4]. Of particular interest among these new quantum states of matter is a large family of two-dimensional (2D) TIs [5–14]. The strong spin-orbit coupling (SOC) in these materials provides the driving force for topological phase transitions; it also lifts the band degeneracy and leads to a spin splitting in inversion-asymmetric systems [15], producing the celebrated Rashba effect [16, 17] that has traditionally been studied in surfaces and interfaces [18], and recently in the layered material BiTeI [19, 20].

Ferroelectricity is an intriguing quantum phenomenon in materials possessing switchable spontaneous polarization. In insulators with strong SOC and inversion asymmetry in the crystal structures, interesting ferroelectric Rashba behavior can be observed [21–23], where the spin texture can be reversed accompanying the ferroelectric switch [24, 25]. Recent studies of GeTe [22] and tin iodide perovskite (FA)SnI3 [26] have shown that the combination of ferroelectricity and SOC leads to a giant Rashba effect with a tunable spin texture via ferroelectric switch [27]. These so called ferroelectric Rashba semiconductors (FERSCs) [27] have been also found in ABC hyper-ferroelectrics (A = Li, Na, K; B = Be, Mg, Ca; C = Sb, Bi) [21, 23, 28]. While FERSCs are normal semiconductors, the associated findings raise the intriguing prospects of having SOC-induced band inversion to accompany the ferroelectric polarization in some properly constructed materials. The coexistence of ferroelectricity and band topology in insulators can occur when SOC is strong enough to induce band inversion in materials that possess spontaneous charge polarization. Such materials have been identified by two groups that reported on the computational discovery of 3D ferroelectric or antiferroelectric TIs in CsPbI3 [29] or orthorhombic AMgBi (A = Li, Na, K) compounds [28].

Recent studies have unveiled several 2D ferroelectric materials, including oxidized MXene (Sc2CO2) [30], SnS [31], and In2Se3 [32, 33]. These 2D systems are highly desirable for their suitability for integration into device design and implementation, and exploration of possible multiple quantum orders in such materials would open new avenues for fundamental research and practical applications. In this paper, we showcase the coexistence of ferroelectric and band topological orders in a 2D functionalized bismuthene. The strong intrinsic SOC in Bi combined with a ligand-induced structural asymmetry in functionalized bismuthene renders this system a 2D ferroelectric TI (FETI). The resulting ferroelectricity is controllable and switchable by a ligand molecule rotation mechanism with a low energy barrier of 0.12 eV. A large spin splitting is
induced by the out-of-plane polarization from the structural symmetry breaking, leading to a quantum valley Hall effect at two nonequivalent K points. The helical spin texture is reversed upon the ferroelectric switch, similar to the results found in FERSCs. These findings make 2D FETIs promising candidates for spintronic applications.

II. METHODS

Structural relaxation and electronic structure calculations were carried out using first-principles methods based on density functional theory (DFT) as implemented in the Vienna Ab initio Simulation (VASP) package [34]. The generalized gradient approximation (GGA) in the Perdew-Burke-Ernzerhof (PBE) [35] form for the exchange and correlation potential, together with the projector-augmented wave (PAW) method, was adopted. The structural model for functionalized bismuthene is periodic in the x-y plane and is separated by at least 10 Å along the z direction to avoid interactions between adjacent layers. All atoms in the unit cell were fully relaxed until the force on each atom was less than 0.01 eV Å\(^{-1}\). The Brillouin zone integration was sampled by 11 × 11 × 1 k-grid mesh for a unit cell, which resulted in good convergence in calculated total energy. An energy cutoff of 400 eV was chosen for the plane wave basis. The van der Waals interaction was described by a semiempirical correction using the Grimme method (DFT-D3) [36]. Spin-orbit coupling (SOC) was included at the second variational step using scalar-relativistic eigenfunctions as a basis. The macroscopic electric polarization of the system was calculated using the Berry phase method, which includes both the ionic and electronic contributions. Energy barriers for phase transitions were calculated using the climbing-image nudge elastic band (CI-NEB) method as implemented in the VASP transition state tools [37]. We have used eight images for energy barrier calculations between two phases, including initial and final positions. The maximally localized Wannier functions (MLWFs) are constructed using the WANNIER90 code within VASP for \(Z_2\) calculations.

III. RESULTS AND DISCUSSION

The ligand-CH\(_2\)OH-functionalized bismuth monolayer (Bi-CH\(_2\)OH for short) is chosen as a prototype 2D FETI to showcase the main characteristics and elucidate the underlying mechanisms. Very recently a 2D bismuth honeycomb lattice was synthesized on top of a SiC substrate [14]; it exhibits a non-trivial gap of 0.8 eV. Surface functionalization of bismuthene using small functional groups (H, F, Cl, Br) further raises the gap to 1 eV [10,38]. This large gap provides a stable platform for ferroelectric order in the system by avoiding a macroscopic depolarization caused by the metallization stemming from temperature or environmental conditions [39]. While ligand-functionalized bismuthene is yet to be realized experimentally, there has been report of covalently functionalized germanane by ligand groups CH\(_2\)OCH\(_3\), CH\(_3\), and CH\(_2\)CHCH\(_2\) [40,41], which provides guidance for the functionalization of bismuthene using similar ligand groups. Even so, it remains a challenge to precisely synthesize ligand-functionalized bismuthene in experiments; the current model is mainly used as a theoretical model to demonstrate the coexistence of ferroelectricity and quantum spin Hall effect in a single 2D material, but is expected to be verified experimentally.

Figure 1 presents the relaxed structure of Bi-CH\(_2\)OH in different configurations, where the Bi atoms adopt a stable \(s^p\) state with the chemical functional groups bonding on both sides of the plane in an alternating way. The paraelectric phase shown in Fig. 1(b) possesses inversion symmetry with point group \(D_{3d}\), therefore exhibiting no spontaneous electric polarization. However, the symmetric configuration is not the most energetically stable. When the H atom of hydroxide on one side is rotated, a more stable configuration is obtained [Fig. 1(a)] while the ligand CH\(_2\)OH on the opposite side remains unchanged. The asymmetric configuration is 0.12 eV lower in energy than the paraelectric phase, but the energy barrier for the H atom rotation is only 6 meV/unit cell [Fig. 2(a)]. Due to the noncentrosymmetry of the structure,
FIG. 3. The band structures of Bi-CH$_2$OH without (red) and with (black) the SOC. (a) Results for the symmetric structure without out-of-plane polarization. (b) Results for the structure with $+P_z$ or $-P_z$ polarization, corresponding to the results shown in Figs. 1(a) and 1(c). The spin-up and -down states are represented by the blue and green lines near the Fermi level, respectively. (c) Spin valley states at the K and K' points. (d), (e) The in-plan spin textures of the conduction bands I and II shown in (b) under polarization $+P_z$ and $-P_z$.

an out-of-plane macroscopic electric polarization is induced, which is $0.223 \times 10^{-10}$ C/m (2.06 μC/cm$^2$) from Berry phase calculations [42,43]. Such a value is larger than 1.60 μC/cm$^2$ in oxidized MXene [30], and an order of magnitude higher than 0.18 μC/cm$^2$ for the 1$T$ phase of MoS$_2$ [44]. Alternatively, when the H atom of hydroxide on the other side of the layer is rotated, the polarization direction is reversed [Fig. 1(c)]. Therefore, starting from the configuration in Fig. 1(a) with spontaneous polarization pointed upward ($+P_z$), one can switch off the polarization in an intermediate state [Fig. 1(b)] by rotating the H atom of hydroxide at the top of the layer after overcoming an energy barrier of 0.12 eV [Fig. 2(a)], then reverse the polarization to $-P_z$ by rotating the H atom of hydroxide on the other side of the layer. The electronic calculations for every image on the NEB path confirm that the structure remains fully gapped during the transition, thus ensuring a smooth polarization reversal as shown in Fig. 2(b).

The electronic structures shown in Fig. 3(a) indicate that the symmetric Bi-CH$_2$OH harbors the topologically insulating order with an indirect band gap of 1.02 eV when the SOC is switched on as confirmed by $Z_2$ topologically invariant calculations. Each SOC band is doubly degenerate because of the structural inversion symmetry. The large nontrivial band gap not only ensures the stable ferroelectricity, but also facilitates the observation of the QSH effect at room temperature. The non-SOC electronic properties are little changed as the spontaneous polarization persists along the $z$ direction induced by the structural symmetry breaking. In contrast, on including the SOC, band degeneracies are lifted in the whole Brillouin zone since the frontier bands near the Fermi level are mainly from the $p_{x,y}$ orbit of Bi (see Fig. 5 in the Appendix), which is sensitive to the out-of-plane polarization. As a result, a characteristic Rashba-like band structure with an obvious Rashba splitting is seen, especially at the $\Gamma$ and M points, and the band gap is reduced to 0.95 eV. Taking the conduction band minimum (CBM) at $\Gamma$ as an example, the Rashba splitting $E_R$ for the ferroelectric structure is 2 meV along $\Gamma$-M with a

Fig. 4. The edge states of (a) the symmetric configuration shown in Fig. 1(b) and 1(b) the ferroelectrically ordered structure shown in Fig. 1(a) or 1(c). The red and blues lines correspond to the edge state from the right and left sides, respectively, while the arrows indicate the spin-up or -down states.
TABLE I. Summary of the functionalized Bi, Pb, and Sb layers with ligand of -CH$_2$OH or -COOH, including the lattice constant $a$, energy barrier for ferroelectric switch $E_{\text{bar}}$, topologically invariant $Z_2$, SOC gap $E_{\text{SOC}}$ of the inversion-symmetric structure, SOC gap $E_{\text{FE}}$ of the asymmetric structure, the vertical polarization $P_z$, the Rashba parameter $\alpha_R$ of CBM at the $\Gamma$ point, the splitting of CBM and VBM at the $K$ point, $\Delta_c$, and $\Delta_v$.

<table>
<thead>
<tr>
<th>Layer</th>
<th>$a$ (Å)</th>
<th>$E_{\text{bar}}$ (eV)</th>
<th>$Z_2$</th>
<th>$E_{\text{SOC}}$ (eV)</th>
<th>$E_{\text{FE}}$ (eV)</th>
<th>$P_z$ ($10^{-10}$ C/m)</th>
<th>$\alpha_R$ (eV Å)</th>
<th>$\Delta_c$ (meV)</th>
<th>$\Delta_v$ (meV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bi-CH$_2$OH</td>
<td>5.497</td>
<td>0.12</td>
<td>1</td>
<td>1.02</td>
<td>0.95</td>
<td>0.223</td>
<td>0.364</td>
<td>72</td>
<td>95</td>
</tr>
<tr>
<td>Bi-COOH</td>
<td>5.497</td>
<td>0.452</td>
<td>1</td>
<td>1.0</td>
<td>0.917</td>
<td>0.204</td>
<td>0.472</td>
<td>26</td>
<td>74.2</td>
</tr>
<tr>
<td>Pb-CH$_2$OH</td>
<td>5.034</td>
<td>0.22</td>
<td>1</td>
<td>0.96</td>
<td>0.784</td>
<td>0.0263</td>
<td>0.737</td>
<td>61.2</td>
<td>25.3</td>
</tr>
<tr>
<td>Pb-COOH</td>
<td>5.034</td>
<td>0.548</td>
<td>1</td>
<td>0.924</td>
<td>0.67</td>
<td>0.2</td>
<td>1.269</td>
<td>80.3</td>
<td>148.9</td>
</tr>
<tr>
<td>Sb-CH$_2$OH</td>
<td>5.258</td>
<td>0.126</td>
<td>1</td>
<td>0.393</td>
<td>0.367</td>
<td>0.256</td>
<td>0.472</td>
<td>26</td>
<td>74.2</td>
</tr>
<tr>
<td>Sb-COOH</td>
<td>5.258</td>
<td>0.364</td>
<td>1</td>
<td>0.882</td>
<td>0.67</td>
<td>0.2</td>
<td>1.269</td>
<td>80.3</td>
<td>148.9</td>
</tr>
</tbody>
</table>

momentum offset of 0.011 Å$^{-1}$. The estimated Rashba parameter $\alpha_R = 0.364$ eV Å; it is comparable to that at the Au surface [45] although smaller than the values for the bulk Rashba compound BiTeI [20]. Although the polarization induces an obvious spin splitting, the band topology is unchanged by the spontaneous polarization as confirmed by $Z_2$. The coexistence of ferroelectricity and band topology is therefore demonstrated in the same 2D material, namely the 2D FETI.

To examine the effect of the ferroelectric switch on key electronic properties, we have presented the helical spin textures of the CBM states for $\pm P_z$ polarization. As seen in Fig. 3(b), the valence and conduction bands are spin split and shifted in the $k$ space away from the $\Gamma$ point in the presence of SOC, therefore resulting in the inner and outer branches. The outer branch shows two symmetric energy minima, while the inner branch displays a cone shape [inset of Fig. 3(b)]. These two split bands present nontrivial and opposite spin textures, with spins orthogonal to the crystal momenta. We have plotted the in-plane spin texture of the two CBMs under $\pm P_z$ polarization, where the direction of $S_{x,y}$ is indicated by arrows. Similarly to FERSCs, the bands show the characteristic Rashba-like spin texture with the two bands having opposite spin orientations, with the inner band having a clockwise spin texture, while the outer branch shows a counterclockwise rotation of spins as one goes around the Brillouin zone center. This spin texture can be reversed by switching the polarization, i.e., by rotating the atomic planes, as shown schematically in the figure. This result offers a feasible way to control and manipulate the spin texture in these materials.

Besides the spin texture reversal, the ferroelectric switch also induces opposite-sign spin splitting at the two nonequi-

FIG. 5. Orbitally resolved band structure of CH$_2$OH-functionalized bismuthene with the polarization of $\pm P_z$, where the red and blue dots represent the states of $p_x$ and $p_y$ of Bi, respectively.

FIG. 6. (a) Energy barriers for the ferroelectric switch in Bi-COOH. The structures of three key symmetric and nonsymmetric Bi-COOH configurations are shown. Electronic band structures of the Bi-COOH layer with SOC off (red) and on (blue) for the structures without (b) and with (c) the out-of-plane polarization. The band topology is preserved throughout the polarization switch process as verified by $Z_2$ calculations, with the nontrivial indirect gap of 1.0 eV (0.917 eV) for symmetric (nonsymmetric) configurations. The vertical polarization is calculated to be $0.204 \times 10^{-10}$ C/m. The blue and green colors near the Fermi level indicate the spin-up and -down state, respectively.
FIG. 7. (a) The energy barrier for the ferroelectric switch of Pb-CH₂OH. Electronic band structures of the Pb-CH₂OH layer with SOC off (red) and on (blue) for the structures without (b) and with (c) the out-of-plane polarization. The vertical polarization is calculated to be $0.263 \times 10^{-11} \text{ C/m}$ when the inversion symmetry is broken. The band topology is preserved with the nontrivial indirect gap of 0.96 eV (0.784 eV) for the symmetric (nonsymmetric) configurations.

...contributions to the quantum Hall conductivity, resulting in a quantum valley Hall (QVH) effect [16]. In contrast to the in-plane spin texture, such QVH effect is robust against the ferroelectric switch since the $S_z$ component is not significantly affected by the out-of-plane polarization.

To calculate the edge states of the 2D FETI state, Bi-CH₂OH with zero and $\pm P_z$ polarization (i.e., the three configurations shown in Fig. 1) are cut into 1D nanoribbons, with their edges passivated with hydrogen to remove the dangling bonds. The calculated results show that the metallic edge states characteristic of TIs are well preserved (Fig. 4); however, there are some changes due to the presence of the ferroelectric order. Differently from the degenerate states in the inversion-symmetric structure without the out-of-plane polarization [Fig. 4(a)], the degeneracy of the edge states is lifted by the ferroelectric order, and the metallic states at two edges are split at the energies indicated by the red and blue lines in Fig. 4(b).

To test the robustness of 2D FETIs, we examined other similarly constructed atomic thin layer structures. For Bi-COOH, the same coexisting multiple quantum orders are obtained as demonstrated by the results summarized in Table I and further supported by Fig. 6 in the Appendix. Compared to Bi-CH₂OH, a significant Rashba effect ($\alpha_R = 0.472 \text{ eV \ Å}$) is obtained at the $\Gamma$ point; however, the energy barrier to achieve the ferroelectric switch is at a higher value of 0.452 eV/unit cell. We also examined Pb/Sb-COOH or Pb/Sb-CH₂OH, as summarized in Table I and supported by Figs. 7–10 in the Appendix; these systems all belong to the same class of 2D FETIs. It should be mentioned that differently from the functionalized Bi layer, the CBM and VBM are located around the $\Gamma$ point for the functionalized Pb layers, and the resulting QVH effect at the K and K’ points would be trivial since the gap is dominated by the states at the $\Gamma$ point as indicated by Fig. 8 in the Appendix. However, the Rashba splitting at the $\Gamma$ point is more pronounced than that in the Bi and Sb layers since the $p_{x,y}$ orbits of Pb near the Fermi level (Fig. 9 in the Appendix) can be considerably affected by the out-of-plane polarization when the inversion symmetry is broken. The Rashba parameter $\alpha_R$ of CBM for the nonsymmetric Pb-COOH is at a large value of 1.269 eV Å, which is comparable to the result for BiTeI [19].

Our extensive calculations show that while details such as the values of the band gap and band splitting depend on the SOC strength of the specific element that makes up the atomically thin layers and also on the choice of the functional ligand groups, all the examined 2D FETIs possess the fundamental TI characteristics and reversible ferroelectric polarization. These findings indicate that coexisting TI and ferroelectric orders is a common phenomenon in these 2D layer systems. It is expected that the same strategy of looking for atomically thin layers and also on the choice of the functional ligand groups, all the examined 2D FETIs possess the fundamental TI characteristics and reversible ferroelectric polarization. These findings indicate that coexisting TI and ferroelectric orders is a common phenomenon in these 2D layer systems. It is expected that the same strategy of looking for atomically thin layers of heavy elements such as Bi, Pb, and Sb functionalized by dipolar molecules such as CH₂OCH₃, CH₂CHCH₂, and their variants can be expanded to other material systems of similar qualities, and their realization is feasible considering that CH₂OCH₃ or CH₂CHCH₂ functionalized germanene has been experimentally synthesized [40,41] and an atomically thin Bi layer also has been experimentally obtained [14], which should facilitate the synthesis of 2D FETIs.

FIG. 8. Orbitally resolved band structures of Pb-CH₂OH layer the SOC off (a) and on (b). Here $p_x$, $p_y$, and $p_z$ are indicated by red, blue, and pink colors, respectively. One can see the band switch between $p_x$ and $p_y$ after the SOC is turned on.
FIG. 9. (a) Energy barriers for the ferroelectric switch of Pb-COOH. Electronic band structures of the Pb-COOH layer with SOC off (red) and on (blue) for the structures without (b) and with (c) the out-of-plane polarization. The vertical polarization is calculated to be $0.2 \times 10^{-10} \text{ C/m}$ when the inversion symmetry is broken. The band topology is preserved with the nontrivial indirect gap of 0.96 eV (0.784 eV) for symmetric (nonsymmetric) configurations.

IV. SUMMARY

In summary, we have introduced 2D FETIs as a class of materials that exhibit coexisting ferroelectric and topologically insulating orders. We have showcased the main characteristics of a prototype 2D FETI system in Bi-CH$_2$OH. Bi-CH$_2$OH exhibits a strong topologically insulating order in all the ferroelectric states, demonstrating a robust coexistence of the two distinct quantum orders in the same system. Furthermore, the interplay between the SOC and symmetry breaking leads to an additional spin valley phenomenon at the K and K' points and a strong Rashba splitting at the M and $\Gamma$ points. These outstanding properties are also verified to be present in other similarly constructed 2D FETIs, and these remarkable quantum states of matter offer a unique platform for further exploration that may open new avenues leading to novel physics discoveries and innovative device applications.

ACKNOWLEDGMENTS

We acknowledge grants of high performance computer time from the computing facility at the Queensland University of Technology, Pawsey Supercomputing Centre, and Australian National Facility. Financial support by the ARC Discovery Early Career Researcher Award (No. DE150101854) is gratefully acknowledged. C.F.C. was partially supported by the US Department of Energy through Cooperative Agreement No. DE-NA0001982.

APPENDIX

The Orbitally resolved band structures of Bi-CH$_2$OH and Pb-CH$_2$OH, the energy barriers of ferroelectric switch of functionalized Bi, Pb, and Sb layers are presented in Figs. 5 –10.

TWO-DIMENSIONAL FERROELECTRIC TOPOLOGICAL …

PHYSICAL REVIEW B 97, 075429 (2018)


[38] Z. Song et al., NPG Asia Mater. 6, e147 (2014).


