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Kondo Signatures of a Quantum Magnetic Impurity in Topological Superconductors

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We study the Kondo physics of a quantum magnetic impurity in two-dimensional topological superconductors (TSCs), either intrinsic or induced on the surface of a bulk topological insulator, using a numerical renormalization group technique. We show that, despite sharing the $p + ip$ pairing symmetry, intrinsic and extrinsic TSCs host different physical processes that produce distinct Kondo signatures. Extrinsic TSCs harbor an unusual screening mechanism involving both electron and orbital degrees of freedom that produces rich and prominent Kondo phenomena, especially an intriguing pseudospin Kondo singlet state in the superconducting gap and a spatially anisotropic spin correlation. In sharp contrast, intrinsic TSCs support a robust impurity spin doublet ground state and an isotropic spin correlation. These findings advance fundamental knowledge of novel Kondo phenomena in TSCs and suggest experimental avenues for their detection and distinction.

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The Kondo problem, which treats a magnetic impurity in metals [1], is a prominent topic in materials research, and its solution by the renormalization group method invokes some of the most profound concepts and techniques in theoretical physics [2]. Kondo phenomena offer insights into impurity scattering and screening processes and reveal characters of host materials. When a magnetic impurity is coupled to electrons in a superconductor (SC), a Yu-Shiba-Rusinov impurity state emerges in the superconducting gap [3,4], reflecting the nature of the SC ground state [5–11]. Classical impurities in topological superconductors (TSCs) [12–18] attracted great interest [19,20] because they exhibit novel physics [21–28] and hold promise for topological quantum computation [29–31]. Among them, two-dimensional (2D) TSCs were predicted to exist by proximity effect on the surface of a topological insulator (TI) [32], which was realized in a $\text{Bi}_2\text{Te}_3/\text{NbSe}_2$ heterostructure [33]. Similar phenomena have been studied in unconventional superconductors $\text{FeTe}_{0.55}\text{Se}_{0.45}$ [34–37] and PbTaSe_2 [38,39]. The proximate s -wave SC mediates an induced $p + ip$ paired TSC state [40], and signatures of

Majorana modes have been observed [33,41]. Intrinsic TSC states also have been explored in layered compound Sr_2RuO_4 [42–46]. While these extrinsic and intrinsic TSCs share the $p + ip$ pairing, they bear fundamental differences in physical properties and underlying mechanisms [47,48].

In this Letter, we study new Kondo physics of a quantum magnetic impurity coupled to intrinsic or extrinsic 2D TSCs using a numerical renormalization group (NRG) technique. We unveil salient features of the ground state of the quantum magnetic impurity in different TSC environments. The Kondo phenomena in extrinsic TSCs are formally equivalent to those in an s -wave superconductor, but unique electronic and orbital coupling schemes drive a distinct screening mechanism that produces new Kondo features, especially a pseudospin singlet state in the superconducting gap and a spatially anisotropic spin correlation. In stark contrast, intrinsic TSCs host a spin doublet ground state and an isotropic spin correlation. These properties define new types of Kondo physics in TSCs and allow

experimental distinction of TSCs driven by different pairing mechanisms.

We consider the standard Anderson impurity model,

$$\hat{H} = \hat{H}_{\text{imp}} + \hat{H}_{\text{hyb}}, \quad (1)$$

$$\hat{H}_{\text{imp}} = \sum_{\sigma} E_f \hat{f}_{\sigma}^{\dagger} \hat{f}_{\sigma} + U \hat{n}_{\uparrow}^f \hat{n}_{\downarrow}^f, \quad (2)$$

$$\hat{H}_{\text{hyb}} = V \sum_{\mathbf{k}\sigma} [\hat{f}_{\sigma}^{\dagger} \hat{c}_{\mathbf{k}\sigma} + \hat{c}_{\mathbf{k}\sigma}^{\dagger} \hat{f}_{\sigma}]. \quad (3)$$

Here, E_f is the local orbital energy and U the Hubbard term, and we take the symmetric case, $E_f = -U/2$, which can be easily generalized to asymmetric cases [49]. The hybridization term is assumed to be independent of momentum and spin. Below we study Kondo physics described by ground-state symmetry, impurity local density of states (LDOS), conduction electron-impurity spin correlation, and impurity susceptibility [50,51].

The intrinsic TSCs with a spinful $p + ip$ pairing symmetry are described by [52]

$$\begin{aligned} \hat{H}_0^i = & - \int d\mathbf{r} \hat{\psi}^{\dagger}(\mathbf{r}) [\nabla^2 / (2m) - \mu] \hat{\psi}(\mathbf{r}) \\ & + \int d\mathbf{r} \frac{\Delta}{2} [\hat{\psi}(\mathbf{r}) \sigma^y (\hat{\partial}_x + i\hat{\partial}_y) \mathbf{d} \cdot \boldsymbol{\sigma} \hat{\psi}(\mathbf{r}) + \text{H.c.}], \end{aligned} \quad (4)$$

where the first part is the kinetic energy of electrons with mass m , and a two-component spinor annihilation operator is defined by $\hat{\psi}(\mathbf{r}) = [\hat{c}_{\uparrow}(\mathbf{r}), \hat{c}_{\downarrow}(\mathbf{r})]^T$; the second part is the pairing energy with a gap Δ and spin operator $\boldsymbol{\sigma}$. The operators $\hat{\partial}_x + i\hat{\partial}_y$ ensure a $p + ip$ pairing, while the vector \mathbf{d} defines an axis, about which \hat{H}_0^i is invariant under the transform $\hat{\psi} \rightarrow e^{i\theta \mathbf{d} \cdot \boldsymbol{\sigma}} \hat{\psi}$ in spin space.

For extrinsic TSCs, the TI surface state with a proximate s -wave pairing is described by

$$\begin{aligned} \hat{H}_0^e = & \int d\mathbf{r} \sum_{\sigma\sigma'} \hat{c}_{\sigma}^{\dagger}(\mathbf{r}) [v_F (-i\boldsymbol{\sigma} \cdot \nabla)_{\sigma\sigma'} - \mu] \hat{c}_{\sigma'}(\mathbf{r}) \\ & + \int d\mathbf{r} \Delta [\hat{c}_{\uparrow}^{\dagger}(\mathbf{r}) \hat{c}_{\downarrow}^{\dagger}(\mathbf{r}) + \text{H.c.}]. \end{aligned} \quad (5)$$

The Dirac-cone state endows an effective $p + ip$ symmetry to the pairing term after a unitary transformation.

We now switch to an orbital angular momentum (OAM) space via $\hat{c}_{\mathbf{k}\sigma} = (1/\sqrt{2\pi k}) \sum_m e^{im\phi} \hat{c}_{m,\sigma}(k)$ with m denoting the OAM, ϕ being the angle of \mathbf{k} with respect to the x axis, and take $\mathbf{d} = \mathbf{e}_z$ [6,53]. In OAM space,

$$\begin{aligned} \hat{H}_0^i = & \int_0^{\infty} dk \left(\sum_{m,\sigma} (k^2/2m - \mu) \hat{c}_{m,\sigma}^{\dagger}(k) \hat{c}_{m,\sigma}(k) \right. \\ & \left. + \Delta [\hat{c}_{0,\uparrow}(k) \hat{c}_{-1,\downarrow}(k) + \hat{c}_{0,\downarrow}(k) \hat{c}_{-1,\uparrow}(k) + \text{H.c.}] \right), \\ \hat{H}_{\text{hyb}}^i = & \frac{\sqrt{NV}}{\sqrt{2\pi}} \int_0^{\infty} dk \sqrt{k} \sum_{\sigma} (\hat{f}_{\sigma}^{\dagger} \hat{c}_{0,\sigma} + \text{H.c.}), \end{aligned} \quad (6)$$

where the intrinsic pairing is between the $m = -1$ and 0 orbits, while the impurity is coupled only to the $m = 0$ orbit. The system always stays in a spin doublet ground state (DGS) even when the Kondo effect dominates over the SC. Once Cooper pairs break up by impurity scattering in the Kondo regime, only electrons with $m = 0$ form the Kondo singlet with the f electron, while $m = -1$ electrons are unpaired, contributing a doubly degenerate spin state coexisting with the Kondo singlet [10].

In the extrinsic case, the Dirac cone term in Eq. (5) locks electronic σ and \mathbf{k} . We introduce $\gamma_{\mathbf{k},\pm} = (c_{\mathbf{k},\uparrow} \pm c_{\mathbf{k},\downarrow} e^{-i\phi})/\sqrt{2}$ to combine the spin-up and spin-down electrons. In OAM space, using $\hat{\gamma}_{\mathbf{k},\alpha} = (1/\sqrt{2\pi k}) \sum_m e^{im\phi} \hat{\gamma}_{m,\alpha}(k)$, we have

$$\begin{aligned} \hat{H}_0^e = & \int_0^{\infty} dk \left\{ \sum_{m,\alpha} (\epsilon_{k\alpha} - \mu) \hat{\gamma}_{m,\alpha}^{\dagger}(k) \hat{\gamma}_{m,\alpha}(k) \right. \\ & \left. + \Delta [\hat{\gamma}_{0,+}^{\dagger}(k) \hat{\gamma}_{-1,+}^{\dagger}(k) + \hat{\gamma}_{-1,-}^{\dagger}(k) \hat{\gamma}_{0,-}^{\dagger}(k)] + \text{H.c.} \right\}, \\ \hat{H}_{\text{hyb}}^e = & \frac{\sqrt{NV}}{2\sqrt{\pi}} \int_0^{\infty} dk \sqrt{k} \{ [\hat{f}_{\uparrow}^{\dagger}(\hat{\gamma}_{0,+}(k) + \hat{\gamma}_{0,-}(k)) \\ & + \hat{f}_{\downarrow}^{\dagger}(\hat{\gamma}_{-1,+}(k) - \hat{\gamma}_{-1,-}(k))] + \text{H.c.} \}, \end{aligned} \quad (7)$$

where $m = -1, 0$ and $\epsilon_{k\alpha} = \alpha v_F k$. Eqs. (6) and (7) contain both $m = -1$ and 0 orbits as essential components in \hat{H}_0^e and \hat{H}_0^i , reflecting the $p + ip$ pairing symmetry in TSCs, while only $m = 0$ orbit is relevant for conventional s -wave SCs [5,6,53]. Moreover, while \hat{H}_{hyb}^i has only $m = 0$ electrons directly coupled to \hat{f}_{σ} in Eq. (6), \hat{H}_{hyb}^e evokes both $m = -1$ and 0 electrons by the unitary transformation. This m dependence of hybridization offers a sensitive probe into the TSC states (see below).

Equations (7) show that the f_{σ} operator is coupled to composite fermion operators $\hat{\gamma}_{0,+}(k) + \hat{\gamma}_{0,-}(k)$ and $\hat{\gamma}_{-1,+}(k) - \hat{\gamma}_{-1,-}(k)$, involving electrons from conduction and valence bands in both spin directions. We introduce a new set of fermionic operators

$$\hat{d}_{\epsilon,\uparrow} = \frac{1}{\sqrt{2}} [\hat{\gamma}_{0,+}(\epsilon)\theta(\epsilon) + \hat{\gamma}_{0,-}(\epsilon)\theta(-\epsilon)], \quad (8)$$

$$\hat{d}_{\epsilon,\downarrow} = \frac{1}{\sqrt{2}} [\hat{\gamma}_{-1,+}(\epsilon)\theta(\epsilon) - \hat{\gamma}_{-1,-}(\epsilon)\theta(-\epsilon)], \quad (9)$$

where $\theta(x)$ is the Heaviside step function and the subscript τ in $\hat{d}_{e,\tau}$ defines a pseudospin, which comprises electronic spin, OAM, and band degrees of freedom from conduction electrons. This implies that two spin-locked bands described by Eq. (5) now are decoupled into two effective, independent bands, each of which is characterized by a pseudospin, but only one effective band is relevant to the Kondo process [54]. Below we use an energy representation [55], where the sum of \mathbf{k} is converted to an integral over energy ϵ in $[-1, 1]$ with the cutoff taken as the energy unit [61], resulting in an effective Hamiltonian

$$\hat{H}_0^e = \int_{-1}^1 d\epsilon \left[\sum_{\tau} g(\epsilon) \hat{d}_{e,\tau}^{\dagger} \hat{d}_{e,\tau} + \Delta (\hat{d}_{e,\uparrow}^{\dagger} \hat{d}_{e,\downarrow}^{\dagger} + \text{H.c.}) \right],$$

$$\hat{H}_{\text{hyb}}^e = \int_{-1}^1 d\epsilon h(\epsilon) \sum_{\tau} [f_{\tau}^{\dagger} \hat{d}_{e,\tau} + \hat{d}_{e,\tau}^{\dagger} f_{\tau}], \quad (10)$$

where $g(\epsilon) = \epsilon - \mu$, $h(\epsilon) = V\rho^{1/2}(\epsilon)/\sqrt{2}$ and $\rho(\epsilon) = N|\epsilon|/2\pi v_F^2$ is the density of states for $\hat{c}_{\mathbf{k},\sigma}$ electrons in the TI surface. An Anderson impurity coupled to an extrinsic TSC with the $p + ip$ pairing is therefore formally equivalent to an impurity coupled to an s -wave SC described by the Eqs. (10). There are, however, some key distinctions [5,6]; e.g., the effective hybridization $h^2(\epsilon) \propto |\epsilon|$ away from the Dirac point and the pseudospin τ accounts for both spin and orbital degrees of freedom from Eqs. (5). Moreover, for $\Delta = 0$, Eqs. (10) reduce to those for the Anderson impurity coupled to the TI surface state [55].

We employed NRG techniques [2,56] to determine low-energy properties of the Anderson impurity in TSCs described by the Hamiltonians derived above, with the effective hybridization coupling $h(\epsilon)$ properly treated for NRG calculations [55,62]. For the most interesting case of $\Delta \neq 0$ and $\mu > \Delta$, the on-site potentials and hopping amplitudes in a Wilson chain adopt a matrix form such that $\hat{d}_{e,\tau}$ fermions are allowed to hop between two nearest sites with different τ [54], following an established logarithmic discretization and numerical diagonalization procedure [2,53]. Key NRG parameters, i.e., the number of preserved states N , number of z averaging N_z , RG scaling parameter Λ , and length of Wilson's chain L_{max} , are provided in the figure captions.

We first examine the lowest-excited energy relative to the ground-state energy $\delta E = E_1 - E_0$ in the thermodynamic limit, which is a key quantity in probing quantum phase transitions driven by U and μ [49,56]. The results for the impurity in extrinsic TSCs exhibit a pattern [Fig. 1(a)] showing that, for a given μ , δE initially declines with increasing U , reaching zero, and then rises again; each δE versus U curve [Fig. 1(b)] has a V shape, and the critical value U_c , where $\delta E = 0$ increases with rising μ . Meanwhile, U_c for an impurity in a conventional s -wave SC is much higher than typical values for extrinsic TSCs,

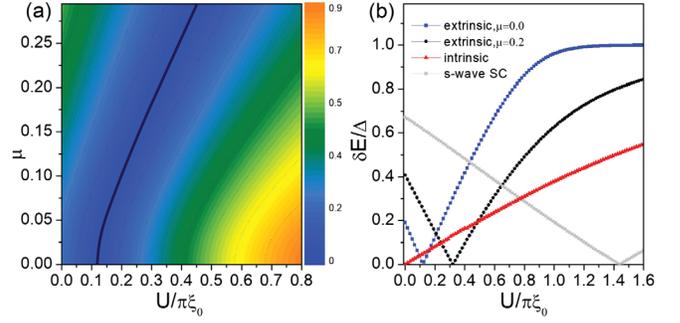


FIG. 1. (a) Phase diagram of δE in μ - U space for extrinsic TSCs. Energy unit is set by the cutoff in Eq. (10), $\Delta = 0.1$, and U is reduced by $\pi\xi_0$, where $\xi_0 = \pi V^2/2$. The transition points where $\delta E = 0$ are highlighted by the dark-blue line. (b) δE versus U at select μ in extrinsic TSCs ($U_c/\pi\xi_0 = 0.11$ and 0.32 for $\mu = 0.0$ and 0.2 , respectively), compared with results for intrinsic TSC ($U_c = 0$) and s -wave SC ($U_c/\pi\xi_0 = 1.44$). NRG parameters used are $N = 400$, $N_z = 10$, $\Lambda = 2.5$, $L_{\text{max}} = 25$.

indicating that U_c is suppressed by the hybridization $h(\epsilon)$ driven by the unique band structure of the proximate TI surface state in extrinsic TSCs. In contrast, intrinsic TSCs display a monotonically increasing δE with $U_c = 0$, indicating an absence of any quantum phase transition in the μ - U space.

To elucidate the behavior of δE , we assess impurity moment $M_{\text{imp}} = \lim_{T \rightarrow 0} \sqrt{T\chi_{\text{imp}}(T)}$, where $\chi_{\text{imp}}(T)$ is impurity susceptibility and T absolute temperature. Calculated M_{imp} in the μ - U space is shown in Fig. 2(a).

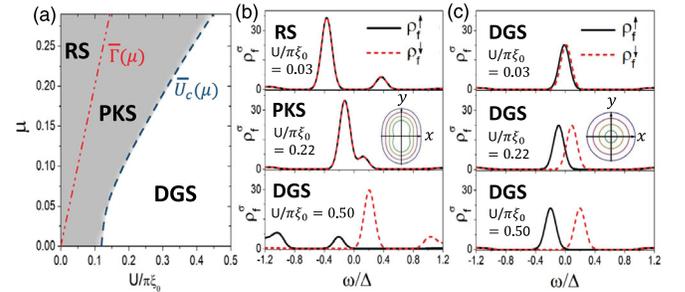


FIG. 2. (a) Phase diagram of M_{imp} in μ - U space for extrinsic TSCs (same energy units as in Fig. 1 and $\Delta = 0.1$). $U_c(\mu)$ sets the phase boundary between $M_{\text{imp}} = 0$ and $M_{\text{imp}} = 1/2$, and $\Gamma(\mu)$ is a crossover boundary between the RS and PKS regimes. Both quantities are reduced by $\pi\xi_0$, as indicated by a bar over each of them. Representative impurity LDOS at $\mu = 0.2$ for (b) the RS, PKS, and DGS ($S_f^z = 1/2$) regimes of extrinsic TSCs and (c) intrinsic TSCs. $\omega = 0$ is at the chemical potential μ of the normal state. Spectral features are broadened in a log-Gaussian scheme with a width factor $b = 0.01$ [63]. Contour plots of spin correlation function $C^x(\mathbf{r})$ in the PKS regime for extrinsic TSCs and in the corresponding DGS regime for intrinsic TSCs are shown as insets. Contour values are -0.10 to -0.07 with a step of 0.01 outward. NRG parameters used are $N = 600$, $N_z = 10$, $\Lambda = 2.5$, $L_{\text{max}} = 25$.

For a fixed μ , the system goes from $M_{\text{imp}} = 0$ at $U < U_c$ to $M_{\text{imp}} = 1/2$ at $U > U_c$, corresponding to a phase transition from a spin singlet to doublet ground state. These results are similar to those in a conventional s wave SC [49]; in contrast, the impurity in intrinsic TSCs stays in the DGS regime at all μ without a phase transition.

At $U > U_c$, Cooper pairs formed by $\hat{d}_{e\tau}$ fermions are robust against impurity scattering, leading to a degenerate \hat{f}_σ -electron doublet state, placing the system in the DGS regime in Fig. 2(a). For $U \leq U_c$, $M_{\text{imp}} = 0$, but the phase space is further divided into two areas separated by a crossover governed by a function $\Gamma(\mu) = \pi V^2 \rho(\mu)$ with $\rho(\mu)$ being the DOS of the normal state at μ . At $0 < U \leq \Gamma$, charge fluctuations of f electrons allow for resonance scattering (RS) between the impurity and conduction electrons [49]; charge fluctuations are greatly suppressed when $U \gg \Gamma$ [54], resulting in the formation of a pseudo-spin Kondo singlet (PKS) state.

In the PKS regime, Cooper pairs are broken by impurity scattering, and pseudospins τ of $\hat{d}_{e\tau}$ fermions released from Cooper pairs form the PKS with the impurity spin. Both the $m = -1, 0$ orbits and spin of conduction electrons $\hat{c}_{m,\sigma}$ are involved in screening the impurity spin. This unusual process produces a spatially anisotropic correlation between the impurity and conduction electron spins [Fig. 2(b)], given by $C^k(\mathbf{r}) = \langle \hat{S}_c^k(\mathbf{r}) \hat{S}_f^k(0) \rangle$, with $k = x, y, z$ and $\hat{\mathbf{S}}_c(\mathbf{r}) = \hat{c}^\dagger(\mathbf{r}) \boldsymbol{\sigma} \hat{c}(\mathbf{r})/2$ and $\hat{\mathbf{S}}_f(0) = \hat{f}^\dagger \boldsymbol{\sigma} \hat{f}/2$ [54]. This feature reflects the spin-momentum locking of the conduction electrons in TI induced extrinsic TSCs, distinguishing the PKS from the conventional Kondo singlet (KS) in normal metals.

We also evaluated impurity LDOS $\rho_f^\sigma(\omega) = -\text{Im}G_f^\sigma(\omega)/\pi$ with $G_f^\sigma(\omega)$ being the Green's function of the f electron with spin σ . We adopted established NRG schemes for spectral densities [64,65], employing the standard log-Gaussian broadening scheme with a width factor $b = 0.01$ [63] on the delta-function-like in-gap spectral features to show clearly the spin degeneracy and states both inside and outside the gap. For the Anderson impurity coupled to a standard s -wave SC, the LDOS in-gap peaks are usually located near $\omega = \pm\Delta$ [49] in the RS regime. Here, for the extrinsic TSC case, $\rho_f^\sigma(\omega)$ is spin independent and has two well-separated peaks in the low- U RS regime. Owing to the effective hybridization $h(\epsilon)$, these peaks move deeper inside the gap toward $\omega = 0$ as seen in Fig. 2(b). At increasing U below U_c , the system undergoes a crossover into the PKS regime, where the two peaks evolve continuously and move closer to $\omega = 0$. For $U > U_c$, the ground state becomes twofold degenerate with $S_f^z = \pm 1/2$ so that Yu-Shiba-Rusinov type in-gap peaks emerge, driven by the scattering between the local moment and Cooper pairs. Different from the RS and PKS regimes, $\rho_f^\uparrow(\omega)$ and $\rho_f^\downarrow(\omega)$ have different profiles in the

DGS regime as shown for the $S_f^z = 1/2$ state in the bottom panel of Fig. 2(b). Meanwhile, the impurity in intrinsic TSCs remains in DGS and its LDOS is less sensitive to parameter changes [Fig. 2(c)]. These distinct LDOS behaviors should be detectable by spin-resolved scanning tunneling microscopy measurements [66], thereby distinguishing extrinsic and intrinsic TSCs.

We now examine the scaling behavior of $T\chi_{\text{imp}}(T)$. For extrinsic TSCs, when $\Delta = 0$ the impurity is coupled to a TI surface state and not screened by conduction electrons for any U at $\mu = 0$ since the Fermi energy is at the Dirac point, whereas it is screened and forms a KS for any $U \neq 0$ as long as $\mu \neq 0$ [50,55]. NRG results for $\Delta = 0$ in Fig. 3(a) indeed show RG flow going to a local-moment (LM) (or DGS) fixed point with $M_{\text{imp}} = 1/2$ for $U \neq 0$ at $\mu = 0$, and to a KS fixed point with $M_{\text{imp}} = 0$ for all U at $\mu \neq 0$. When $\Delta \neq 0$, the RG flow goes to fixed points with $M_{\text{imp}} = 0$ and $1/2$ for $U < U_c$ and $U > U_c$, respectively, even at $\mu = 0$ as shown in Fig. 3(b) [67]. In this case, the impurity is screened by the $\hat{d}_{e\tau}$ fermions released from the Cooper pairs for sufficiently low T and $U < U_c$. When $\mu \neq 0$, in addition to the fixed points at $\mu = 0$, an RS fixed point with $M_{\text{imp}} = 0$ appears at $U \leq \Gamma$ as shown in Fig. 3(c). Although the PKS and RS fixed point can hardly be distinguished by $T\chi_{\text{imp}}(T)$, they manifest themselves by different locations of in-gap LDOS peaks. It should be noted that NRG calculations of $T\chi_{\text{imp}}(T)$ are sensitive to computational procedures [68] and NRG parameters [6,64], especially at $T \sim \Delta$. We have performed extensive

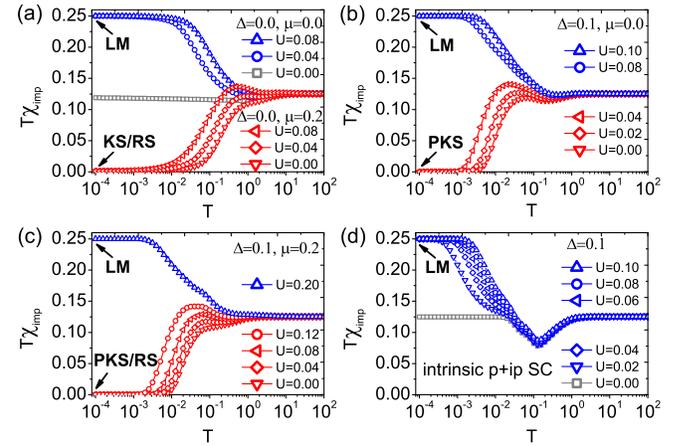


FIG. 3. The scaling behavior of $T\chi_{\text{imp}}(T)$ for the impurity in (a)–(c) extrinsic and (d) intrinsic TSCs. (a) At $\Delta = 0$, the RG flow goes to a LM fixed point with $M_{\text{imp}} = 1/2$ for $\mu = 0$ and, when $\mu \neq 0$, to KS and RS fixed points with $M_{\text{imp}} = 0$ for $U \neq 0$ and $U = 0$, respectively. (b) At $\Delta \neq 0$ and $\mu = 0$, the RG flow goes to $M_{\text{imp}} = 1/2$ (LM) and 0 (PKS) fixed points for $U > U_c$ and $U < U_c$, respectively. (c) At $\Delta \neq 0$ and $\mu \neq 0$, an additional RS fixed point with $M_{\text{imp}} = 0$ appears. (d) RG flows go to the LM fixed point for $U \neq 0$ at all μ . NRG parameters used are $N = 600$, $N_z = 10$, $\Lambda = 1.8$, $L_{\text{max}} = 15$.

calculations and analysis to choose suitable parameters [54]. For comparison, we also show $T\chi_{\text{imp}}(T)$ for the impurity in intrinsic TSCs in Fig. 3(d), where only the LM fixed point with $M_{\text{imp}} = 1/2$ exists for all $U \neq 0$. These results highlight fundamentally different Kondo physics in intrinsic and extrinsic TSCs.

Summary and discussion.—We have shown a new type of Kondo phenomena associated with a quantum magnetic impurity coupled to extrinsic 2D $p + ip$ TSCs, involving a pseudospin Kondo singlet with a spatially anisotropic spin correlation, which is fundamentally distinct from the intrinsic case that may host only a conventional Kondo singlet with an isotropic spin correlation. This work provides a protocol for probing new physics of quantum magnetic impurity in a wide range of TSC models [21–23,57–60,69–77]. For instance, when 1D helical edge states of a quantum spin Hall insulator is coupled to an s -wave SC with an external Zeeman field [57], the left and right movers are mixed and play the role of pseudospins [54] that participate in the Kondo screening processes. Similarly, for 3D superconducting Weyl metals [58–60,77], the effective $p + ip$ symmetry pairing and thus the $m = -1, 0$, orbits are induced by the chiral nature of the Weyl nodes such that both orbits screen the impurity together with the electron spins [54], which would result in anisotropic spin-spin correlation in the Kondo regime. In contrast, this type of Kondo state would not show up in a topologically trivial SC-like graphene on an s -wave SC substrate, where only a traditional Kondo singlet can be found [54].

Recently, spin-polarized Yu-Shiba-Rusinov states were observed by spin-resolved spectroscopy measurements in a conventional s -wave superconductor [66]. Such experimental probes should be applicable for measuring the impurity LDOS and spin susceptibility in $\text{Bi}_2\text{Te}_3/\text{NbSe}_2$ heterostructure [33,41], where a 2D extrinsic $p + ip$ symmetry pairing SC state is present in the surfaces of the Bi_2Te_3 TI thin film of several quintuple layers via the proximity effect with the NbSe_2 SC substrate. In addition, STM/STS measurements may also be properly devised to detect tunneling current of an Anderson impurity. Furthermore, $\text{FeTe}_{0.55}\text{Se}_{0.45}$ [34–37] or PbTaSe_2 [38,39] may provide a natural platform to detect the novel Kondo effects. Our findings are therefore expected to have major implications for further exploration of novel quantum magnetic impurity effects in realistic electronic environments involving either effective or equivalent spin-orbital couplings.

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